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An efficient user identification scheme based on ID-based cryptosystem

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Abstract

Tseng-Jan modified a non-interactive public key distribution system and also proposed several applications based on the Maurer–Yacobi scheme. In their scheme, a user can prove his identity to another user without revealing his secret key. They use a challenge-response-type interactive protocol to achieve their objective. However, in wireless environment, waiting for a corresponding response from the other is time-wasting and consumes the battery of the mobile device. The ability of computing and the capacity of the battery of a mobile device are limited. Therefore, we propose an efficient scheme based on ID-based cryptosystem that is more suitable to be applied in the mobile environment.

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Keywords: Challenge-response protocol; Identity-based cryptosystem; User identification

1. Introduction

Shamir proposed a concept based on a public key cryptosystem in 1984 that can let each user's identification information be his public key [4]. Each user has the ability to verify the signature without exchanging his secret and public keys and without using the services of a third party. In other words, the user uses a unique identification information (e.g., name, address and e-mail address) as his public key, so that it is impossible for him to deny that the public key does not belong to him. Many identity-based public key systems have been

proposed based on Shamir's idea [1,2,6]. In these schemes, the trusted authority center holds the secret number and decides whether the secret is locked by the receiver. In other words, the public user's ID is not his real identification information. To public user's secrets or not is decided by the trusted authority center.

In 1991, Maurer–Yacobi proposed an identity-based non-interactive public key distribution system based on a novel trapdoor one-way function of exponentiation modulo a composite number. They released the final version in 1996 [3]. Users are verified by their identity information without doing an interactive public key authentication. They adopted the squaring method and the Jacobi symbol method to ensure that each identity number corresponds to the identification information. In their scheme, there are no public keys,

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50 certificates or other information. Each user applies his/
51 her information as the public key.

52 Tseng–Jan improved the squaring method based on
53 the Maurer–Yacobi scheme and also proposed a user
54 identification scheme [5]. However, in the wireless
55 environment, the capacity of the battery of a mobile
56 device is limited. The time for waiting and responding
57 must be reduced. Therefore, we propose an improved
58 scheme that is suitable for the wireless environment.

59 The remainder of the article is organized as fol-
60 lows. In Section 2, we briefly review Tseng–Jan’s
61 user identification scheme. In Section 3, the improved
62 scheme proposed by us is presented. In Section 4, we
63 analyze the security of our improved scheme. In
64 Section 5, we discuss the efficiency and the security
65 of our scheme. Finally, we give a brief conclusion in
66 Section 6.

67 **2. Review of Tseng–Jan’s scheme**

68 Tseng–Jan proposed a user identification scheme
69 using a challenge-response-type interactive protocol.
70 A trusted authority in their scheme is used to generate
71 system parameters as follows: N denotes the product
72 of four primes p_j , whose decimal digits are between
73 60 and 70; the numbers $(p_j - 1)/2$ are odd and
74 pairwise relatively prime; e denotes an integer in
75 $Z_{\phi(N)}^*$ and the secret d , which satisfies $ed \equiv 1 \pmod{\phi(N)}$;
76 t denotes a random number from $Z_{\phi(N)}^*$, where
77 ϕ is the Euler’s totient function; g is a primitive
78 element in $GF(p_j)$; and $h(\cdot)$ is a one-way function.

79 When a user Alice joins the system, she presents
80 her unique identity ID_a to the trusted authority. The
81 trusted authority then computes $s_a = et \log_g(ID_a^2) \pmod{\phi(N)}$
82 and sends s_a to Alice as her secret key in secret.
83 The trusted authority publishes $\{N, g, e, h(\cdot)\}$ and keeps
84 $\{p_1, p_2, p_3, p_4, t, v, d\}$ secret for all users. And the legal
85 user, Alice, publishes $\{ID_a\}$ and keeps $\{s_a\}$ secretly.

86 The scheme can be shown as Fig. 1 when Alice
87 wants to show her identity to the verifier Bob.

88 Step 1. Alice sends her identity, ID_a , to the verifier
89 Bob.

90 Step 2. Bob chooses a random integer k in Z_N^* and
91 sends Y to Alice by computing $Y = (ID_b^2)^k \pmod N$.

92 Step 3. After receiving Y , Alice computes $Z = Y^{s_a}$
93 $\pmod N$ and sends Z to Bob.

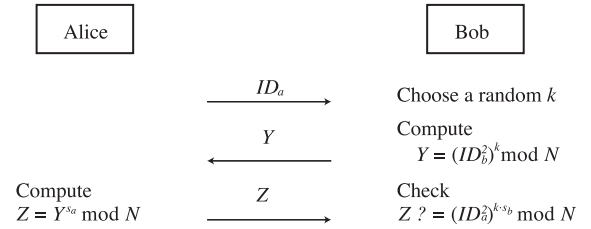


Fig. 1. Tseng–Jan’s user identification scheme.

Step 4. In order to identify validity of Alice, Bob 94
verifies the equation 95
96

$$Z ? = (ID_a^2)^{k s_b} \pmod N. \quad (1)$$

If the equation holds, Bob will confirm that Alice’s 98
identity is valid. 99

In their scheme, Bob just uses Alice’s identity ID_a 100
as her public key to check the verification equation. 101
From the above description of their scheme, Alice 102
then sends out her identity ID_a and makes the corre- 103
spondent response to Bob in Steps 1 and 3. However, 104
the problem of using their scheme is that they waste 105
too much time waiting for the responses. In next 106
section, our improved scheme is shown in which there 107
is only one pass verification. 108

3. The proposed scheme 109

Our scheme still inherits the advantage of 110
Tseng–Jan’s scheme that the user’s identity is his/ 111
her public key. Furthermore, we only use one pass 112
to show the validity of user’s identity. The param- 113
eters $\{N, g, e, d, t, v, p_1, p_2, p_3, p_4\}$ are the same as those 114
in Tseng–Jan’s scheme. The notation is the bits 115
connection. We add one notation T for the timestamp. 116
Assuming the situation that the mobile device (M_1) 117
wants to show his identity (ID_m) is legal to the base 118
station (BS). The identity of BS is ID_b . We illustrate 119
this scheme in Fig. 2. 120

Step 1. Mobile device (M) chooses a random 121
integer k in Z_N^* and computes Y and Z as follows: 122

$$Y = (ID_m^2)^k \pmod N,$$

$$Z = (ID_b^2)^{k s_m T} \pmod N.$$

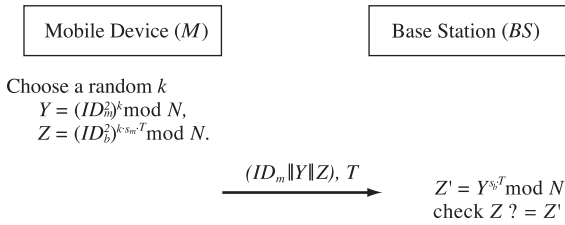


Fig. 2. The proposed scheme suitable for the wireless environment.

127 Then, he sends $\{(ID_m || Y || Z), T\}$ to the base station
 128 (BS).

129 Step 2. After receiving the above messages from
 130 *M*, BS computes $Z' = Y^{s_b^T} \bmod N$.

131 Step 3. BS checks the equation $Z' = Z$. If the
 132 equation holds, BS will confirm that *M*'s identity is
 133 validity.

134 In Tseng–Jan's scheme, three passes were need-
 135 ed to show the identity and the transmitted mes-
 136 sages between two parties are $\{ID_a, Y, Z\}$. All the
 137 transmitted messages in our scheme are the same as
 138 those in Tseng–Jan's system, except the additional
 139 value, timestamp *T*. However, the proposed scheme
 140 needs only one pass to show the valid identity. We
 141 reduce the time used for responding and waiting so
 142 that the limited capacity of the battery of a mobile
 143 device will no longer be a problem. Thus, the
 144 proposed scheme is more efficient than Tseng–Jan's
 145 scheme.

146 4. Performance analysis

147 In this section, we present the performance of our
 148 proposed scheme. It is just as the analysis of the
 149 computational complexity of Tseng–Jan's scheme.
 150 Unfortunately, in their scheme, a great deal of running
 151 time is spent in waiting the responded value. Our
 152 scheme adds an extreme parameter to let the scheme
 153 be more efficient.

154 In their scheme, the user (Alice) proves her
 155 identity to the verifier (Bob), she has to spend much
 156 time waiting for obtaining *Y* from Bob in Step 2
 157 because without getting *Y*, she cannot work. When
 158 the network congests, Alice may consume most of
 159 her device battery in waiting the responded value.
 160 She may also idle and exhaust the battery when she
 161 cannot get the responded value. However, our im-

proved scheme can reduce the time for waiting. 162
 What the user (*M*) needs to do is only to send the 163
 message $\{(ID_m || Y || Z), T\}$ to the verifier (BS). 164
 Therefore, our scheme can save the limited capacity 165
 of the battery of the mobile device. 166

Since the mobile device (*M*) wants to identify and 167
 his identity to transmit the message to the base 168
 station (BS) of our scheme, it requires 1 pass. In 169
 the phase of waiting responded value of our scheme, 170
M need not spend any waiting time to require the 171
 value. The notation $|X|$ denotes the bit-string length 172
 of transmitted message. Total transmitted messages 173
 in this scheme require $|ID| + |Y| + |Z| + |T|$. All 174
 of our transmitted messages are the same as those in 175
 Tseng–Jan's scheme except *T* which is much 176
 smaller. Moreover, our improved scheme takes less 177
 power by reducing the waiting time. Hence, our 178
 scheme is more suitable to be used in wireless 179
 environment. 180

181 5. Security analysis

182 Tseng–Jan's scheme is based on the Maurer– 182
 Yacobi scheme with an additional message. In the 183
 system setup phase, computing a discrete logarithm 184
 modulo prime *N* without knowing the prime factors of 185
N is still infeasible. Our scheme is the same as Tseng– 186
 Jan's scheme on this point. Therefore, to compute the 187
 composite number *N* just means to face the difficult 188
 factoring problem. 189

In the following, some attacks are presented. 190

191 Attack 1: The intruder can obtain $\{Y, Z, T\}$, which 191
 are the transmitted messages between *M* and BS. 192
 However, computing *M*'s secret key s_m from 193
 $Z = (ID_m^k) s_m^T \bmod N$ is a difficult factoring 194
 problem. 195

196 Attack 2: Let *g* be a generator in the range between 196
 0 and *N* – 1, where *N* is a composite number. Let 197
 $y = g^x \bmod N$. The Discrete Logarithm Problem is 198
 to find *x* from *y*. If the intruder wants to obtain the 199
 random number *k* from $Y = (ID_m^k) \bmod N$, he will 200
 face the problem of solving the discrete logarithm 201
 problem. If he further chooses a random number 202
k' to forge $\{ID_m || Y_{int} || Z_{int}\}$, he will fail in 203
 making *Zint* to pass the receiver's verification 204
 without correct s_m and *k*. 205

206 Attack 3: The intruder further adopts replay
 207 attack. He intercepts the message $\{(ID_m \parallel Y \parallel Z),$
 208 $T\}$ from network during the legal user ID_m sends
 209 it to the user ID_b . After a span time, he may
 210 pretend to be the user ID_m to re-send the message
 211 to the user ID_b . However, he will fail, because Z
 212 includes a timestamp T . To replace a new time
 213 stamp in Z also requires solving the difficult
 214 factoring problem.

215 6. Discussion

216 In this section, we discuss the efficiency and
 217 security of our scheme as follows.

219 6.1. Advantage of the parallel processing

220 In Tseng–Jan’s scheme, there are three modular
 221 exponentiations in Steps 2, 3 and 4, respectively. We
 222 also need to execute three modular exponentiations to
 223 verify the user identification in Steps 1 and 2. How-
 224 ever, when the device has two or more CPU, he can
 225 compute two equations in Step 1 in parallel, but
 226 Tseng–Jan’s scheme cannot. Therefore, we can short-
 227 en the total computing time by using parallel process-
 228 ing technique.

230 6.2. Reduce the communication time and the cost

231 Tseng–Jan’s scheme still needs three times of
 232 transmission. On the contrary, we only need handle
 233 it once. Both the user and verifier do not cost any time
 234 to wait for responding. Therefore, the communication
 235 time and transmission cost are decreased.

237 6.3. Ability of resisting the denial of service attack

238 Tseng–Jan’s scheme cannot withstand the denial of
 239 service attack. Any malicious attacker can send a
 240 forged ID_i in Step 1 and any value Z_i in Step 3. The
 241 verifier ID_b should execute two modular exponentia-
 242 tions and one comparison to verify the identity. The
 243 ID_b could be weighed down with the heavy comput-
 244 ing work and crashed. Nevertheless, in our scheme,
 245 the ID_b just needs to receive all the messages from the
 246 other user once. The verifier ID_b can verify the
 247 identity right away.

6.4. Economy of memory resource

In Tseng–Jan’s scheme, the verifier must cost
 more storage memory to save random numbers and
 users’ identities until after finishing the identification.
 Evidently, our scheme does not require any storage
 memory to do so.

7. Conclusions

We proposed an efficient scheme based on Tseng–
 Jan’s scheme. Compared with their scheme, our
 reduce the time for responding and waiting. Also,
 our scheme uses the user’s identity as his public key
 and does not need a key directory to store users’ keys.

Our improved scheme costs less computing
 time and waiting time. Therefore, our scheme is
 more suitable to be employed in wireless network
 applications.

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